

解説

1 $2A + B - (4A - 3B) = 2A + B - 4A + 3B = -2A + 4B$
 $= -2(2x^2 - 4x - 5) + 4(3x^2 - 2x + 2)$
 $= -4x^2 + 8x + 10 + 12x^2 - 8x + 8$
 $= (-4 + 12)x^2 + (8 - 8)x + (10 + 8)$
 $= 8x^2 + 18$

解説

2 与式 $= ax(x^2 - x + a) - (x^2 - x + a)$
 $= ax^3 - ax^2 + a^2x - x^2 + x - a$
 $= ax^3 - (a + 1)x^2 + (a^2 + 1)x - a$

解説

- 3 (1) 与式 $= a^2 - 2 \cdot a \cdot 3b + (3b)^2 = a^2 - 6ab + 9b^2$
 (2) 与式 $= (-a)^2 - b^2 = a^2 - b^2$
 (3) 与式 $= x^2 + (-4 + 2)x + (-4) \cdot 2 = x^2 - 2x - 8$
 (4) 与式 $= x^2 + \{(-2y) + (-13y)\}x + (-2y) \cdot (-13y)$
 $= x^2 - 15y \cdot x + 26y^2$
 $= x^2 - 15xy + 26y^2$
 (5) 与式 $= 3 \cdot 4x^2 + \{3 \cdot 3 + (-2) \cdot 4\}x + (-2) \cdot 3$
 $= 12x^2 + x - 6$
 (6) 与式 $= 2 \cdot 3a^2 + \{2 \cdot (-2) + (-1) \cdot 3\}ab + (-1) \cdot (-2)b^2$
 $= 6a^2 - 7ab + 2b^2$
 (7) 公式 $(a + b + c)^2 = a^2 + b^2 + c^2 + 2ab + 2bc + 2ca$ を適用すると、次のように展開できる。
 与式 $= x^2 + y^2 + (-1)^2 + 2 \cdot x \cdot y + 2 \cdot y \cdot (-1) + 2 \cdot (-1) \cdot x$
 $= x^2 + 2xy + y^2 - 2x - 2y + 1$
 (8) 与式 $= \{(x^2 - 4) + 2x\}\{(x^2 - 4) - 2x\} = (x^2 - 4)^2 - (2x)^2$
 $= x^4 - 8x^2 + 16 - 4x^2 = x^4 - 12x^2 + 16$
 (9) 与式 $= \{(a + 2b)(a - 2b)\}^2 = (a^2 - 4b^2)^2$
 $= (a^2)^2 - 2 \cdot a^2 \cdot 4b^2 + (4b^2)^2$
 $= a^4 - 8a^2b^2 + 16b^4$
 (10) 与式 $= (x^2 - y^2)(x^2 + y^2)(x^4 + y^4)$
 $= (x^4 - y^4)(x^4 + y^4)$
 $= x^8 - y^8$
 (11)
 与式 $= (x + 1)(x - 4) \times (x - 1)(x - 2) = (x^2 - 3x - 4)(x^2 - 3x + 2)$
 $= \{(x^2 - 3x) - 4\}\{(x^2 - 3x) + 2\} = (x^2 - 3x)^2 - 2(x^2 - 3x) - 8$
 $= x^4 - 6x^3 + 9x^2 - 2x^2 + 6x - 8 = x^4 - 6x^3 + 7x^2 + 6x - 8$
 (12) 与式 $= a^3 - 3 \cdot a^2 \cdot 2 + 3 \cdot a \cdot 2^2 - 2^3 = a^3 - 6a^2 + 12a - 8$
 (13) 与式 $= (x - 1)(x^2 + x \cdot 1 + 1^2) = x^3 - 1^3$
 $= x^3 - 1$

解説

- 4 (1) 与式 $= 3ab \cdot 2a + 3ab \cdot b = 3ab(2a + b)$
 (2) 与式 $= (a - 1)(x - 1)$
 (3) 与式 $= x^2 - 2 \cdot x \cdot 4 + 4^2 = (x - 4)^2$
 (4) 与式 $= (2x)^2 - (5y)^2 = (2x + 5y)(2x - 5y)$
 (5) 与式 $= x^2 + (-5 - 7)x + (-5) \cdot (-7) = (x - 5)(x - 7)$
 (6) $3x^2 + 5x + 2 = (x + 1)(3x + 2)$

$$\begin{array}{r} 1 \times 1 \rightarrow 3 \\ 3 \times 2 \rightarrow 2 \\ \hline 3 \quad 2 \quad 5 \end{array}$$

 (7) $6x^2 + x - 1 = (2x + 1)(3x - 1)$

$$\begin{array}{r} 2 \times 1 \rightarrow 3 \\ 3 \times -1 \rightarrow -2 \\ \hline 6 \quad -1 \quad 1 \end{array}$$

(8) $2a^2 - 7ab + 6b^2 = (a - 2b)(2a - 3b)$

$$\begin{array}{r} 1 \times -2b \rightarrow -4b \\ 2 \times -3b \rightarrow -3b \\ \hline 2 \quad 6b^2 \quad -7b \end{array}$$

(9) $12x^2 - 7xy - 12y^2 = (3x - 4y)(4x + 3y)$

$$\begin{array}{r} 3 \times -4y \rightarrow -16y \\ 4 \times 3y \rightarrow 9y \\ \hline 12 \quad -12y^2 \quad -7y \end{array}$$

(10) $12x^2 - 23xy + 10y^2 = (3x - 2y)(4x - 5y)$

$$\begin{array}{r} 3 \times -2y \rightarrow -8y \\ 4 \times -5y \rightarrow -15y \\ \hline 12 \quad 10y^2 \quad -23y \end{array}$$

(11) 与式 $= \{(x - y) - 4\}\{(x - y) + 6\} = (x - y - 4)(x - y + 6)$

(12) 与式 $= (2x)^2 - (y + z)^2 = \{2x + (y + z)\}\{2x - (y + z)\}$
 $= (2x + y + z)(2x - y - z)$

(13) 与式 $= (x^2)^2 + 4x^2 - 5 = (x^2 - 1)(x^2 + 5)$
 $= (x + 1)(x - 1)(x^2 + 5)$

(14) 与式 $= (x^2)^2 - 13x^2 + 36 = (x^2 - 4)(x^2 - 9)$
 $= (x + 2)(x - 2)(x + 3)(x - 3)$

(15) 与式 $= x(y - 1) - (y - 1) = (x - 1)(y - 1)$

(16) 与式 $= (2x - 8)y + (x^2 - 16) = 2(x - 4)y + (x + 4)(x - 4)$
 $= (x - 4)\{2y + (x + 4)\} = (x - 4)(x + 2y + 4)$

(17) 与式 $= x^2 + (5y - 2)x + (6y^2 - 7y - 3)$
 $= x^2 + (5y - 2)x + (2y - 3)(3y + 1)$
 $= \{x + (2y - 3)\}\{x + (3y + 1)\}$
 $= (x + 2y - 3)(x + 3y + 1)$

$$\begin{array}{r} 1 \times 2y - 3 \rightarrow 2y - 3 \\ 1 \times 3y + 1 \rightarrow 3y + 1 \\ \hline 1 \quad (2y - 3)(3y + 1) \quad 5y - 2 \end{array}$$

(18) 与式 $= 2x^2 + (5y + 5)x + (2y^2 + y - 3)$
 $= 2x^2 + (5y + 5)x + (y - 1)(2y + 3)$
 $= \{x + (2y + 3)\}\{2x + (y - 1)\}$
 $= (x + 2y + 3)(2x + y - 1)$

$$\begin{array}{r} 1 \times 2y + 3 \rightarrow 4y + 6 \\ 2 \times y - 1 \rightarrow y - 1 \\ \hline 2 \quad (y - 1)(2y + 3) \quad 5y + 5 \end{array}$$

(19) 与式 $= a^2b + ab^2 + b^2c + bc^2 + c^2a + ca^2 + 3abc$
 $= (b + c)a^2 + (b^2 + c^2 + 3bc)a + bc(b + c)$
 $= \{a + (b + c)\}\{(b + c)a + bc\}$
 $= (a + b + c)(ab + bc + ca)$

$$\begin{array}{r} 1 \times b + c \rightarrow b^2 + 2bc + c^2 \\ b + c \times bc \rightarrow bc \\ \hline b + c \quad bc(b + c) \quad b^2 + c^2 + 3bc \end{array}$$

(20) 与式 $= x^3 + 3^3 = (x + 3)(x^2 - x \cdot 3 + 3^2)$
 $= (x + 3)(x^2 - 3x + 9)$

(21) 与式 $= (2x)^3 - y^3 = (2x - y)\{(2x)^2 + 2x \cdot y + y^2\}$
 $= (2x - y)(4x^2 + 2xy + y^2)$

(22) 与式 $= (x^4 - 8x^2 + 16) - x^2 = (x^2 - 4)^2 - x^2$
 $= \{(x^2 - 4) + x\}\{(x^2 - 4) - x\}$
 $= (x^2 + x - 4)(x^2 - x - 4)$